



College of  
ENGINEERING, COMPUTING  
AND APPLIED SCIENCES

# Simulating the Tradespace with Synthetic Data

*AI4SE/SE4AI Workshop*

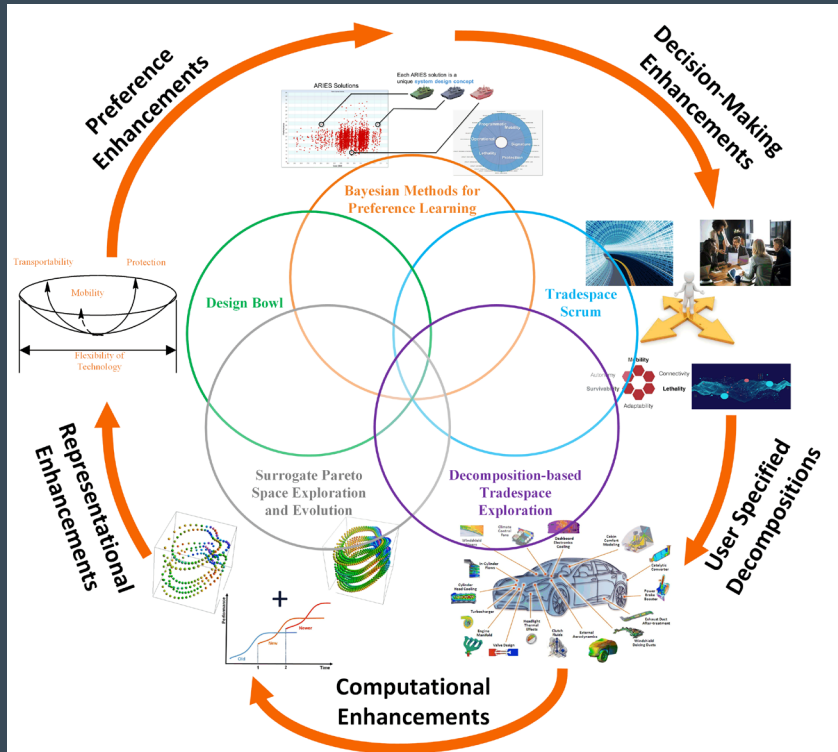
*Dr. Cameron J. Turner*

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CLEMSON  
**VIPR-GS**  
VIRTUAL PROTOTYPING  
GROUND SYSTEMS

# Project Context



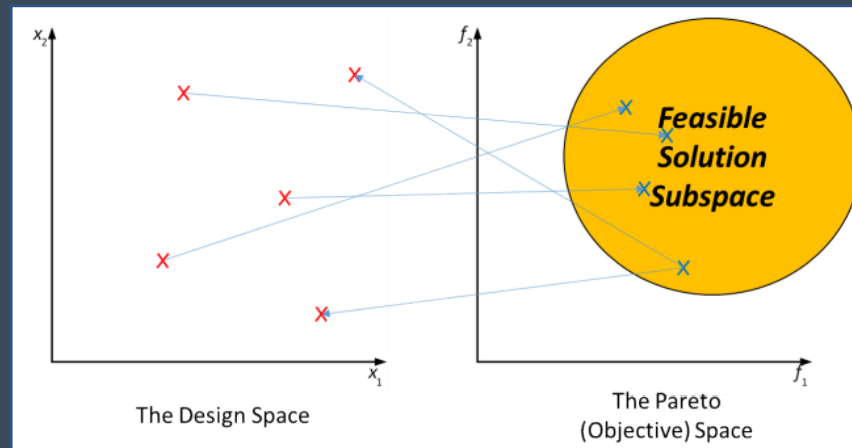
- **Scope:** Enhance the abilities of stakeholders to balance vehicle performance or capabilities versus project risk, budget, and schedule in a visual virtual environment
- **Key Goal:** Enhance rapid, effective trade space exploration and analysis to guide the development of vehicle-level requirements
- **Efforts in:**
  - Decomposition-Based Tradespace Exploration
  - Surrogate Pareto Space Exploration and Evolution
  - Design “Bowl” Modeling
  - Bayesian Methods for Preference Learning
  - Best-Practices in Tradespace Scrums

# The Tradespace

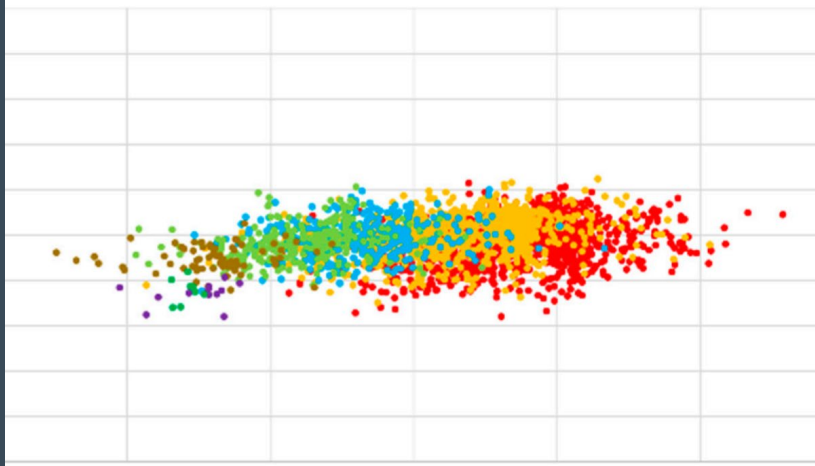
Function	Soln 1	Soln 2	...	Soln N
Convert	100 hp ICE	120 hp ICE	...	50 hp Hub Motors
Store	10 gal JP7	15 gal JP7	...	1kW-hr Battery
...	...	...	...	...
Convert	4-Wheels	6-Wheels	...	Oval Tracks

- Each point in the Tradespace represents a solution to a Morphological Matrix

- The Tradespace is visualized in terms of an objective space



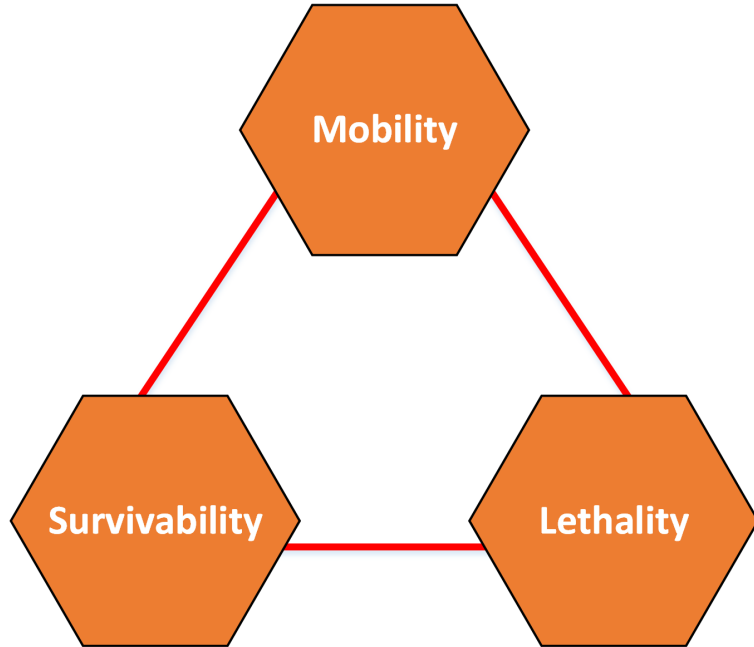
# Tradespace Modeling



- Generating a representation of the Tradespace has been a significant effort

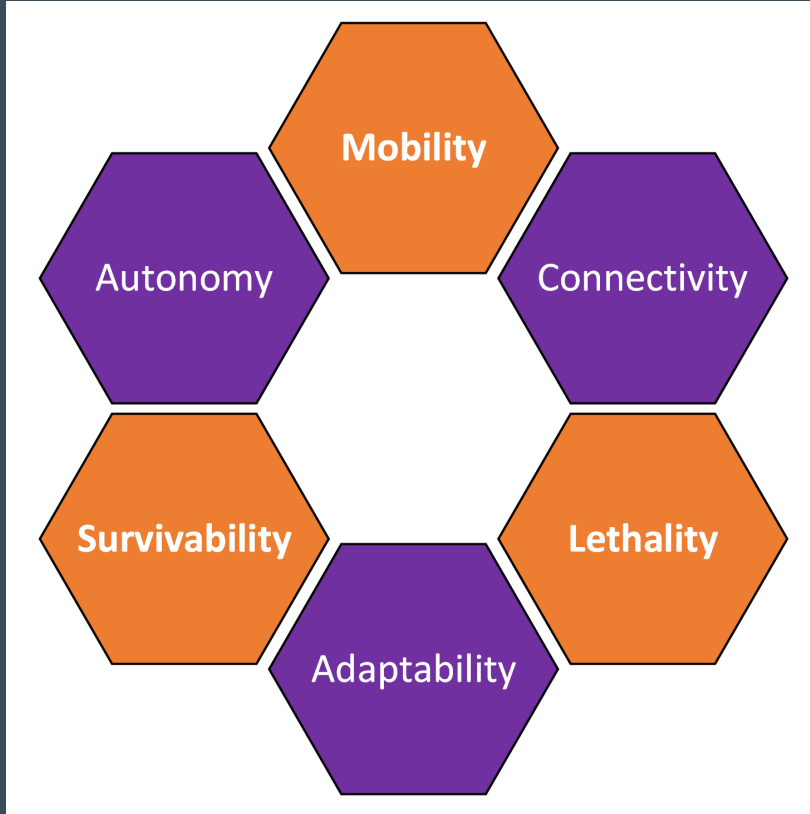
- Need to represent “-ilities”
  - Functional Objectives (FO)
  - Input Variables
  - Derived Attributes
  - Intermediate Calculated Parameters
  - Defined Constants
  - Other FO

# “-ilities”



- Represent subsets of the considerations of the Steel Hexagon
  - Developed from the concept of the Steel Triangle
  - Mobility – Survivability – Lethality

# “-ilities”



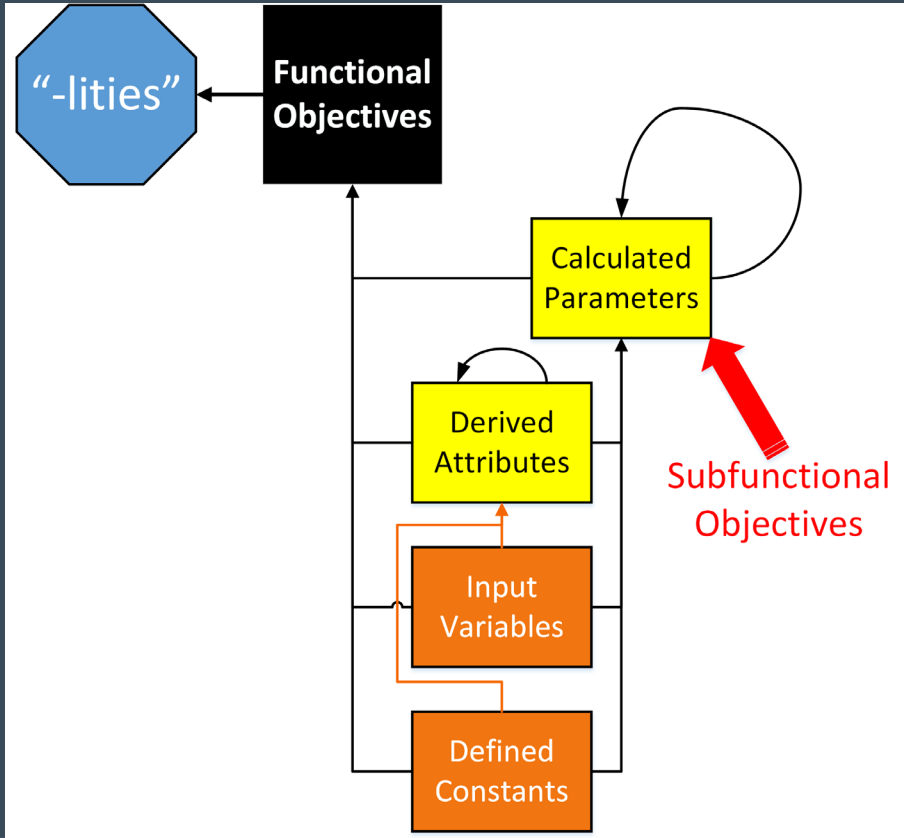
- Represent subsets of the considerations of the Steel Hexagon
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  - Add – Autonomy – Connectivity - Adaptability

# “-ilities”



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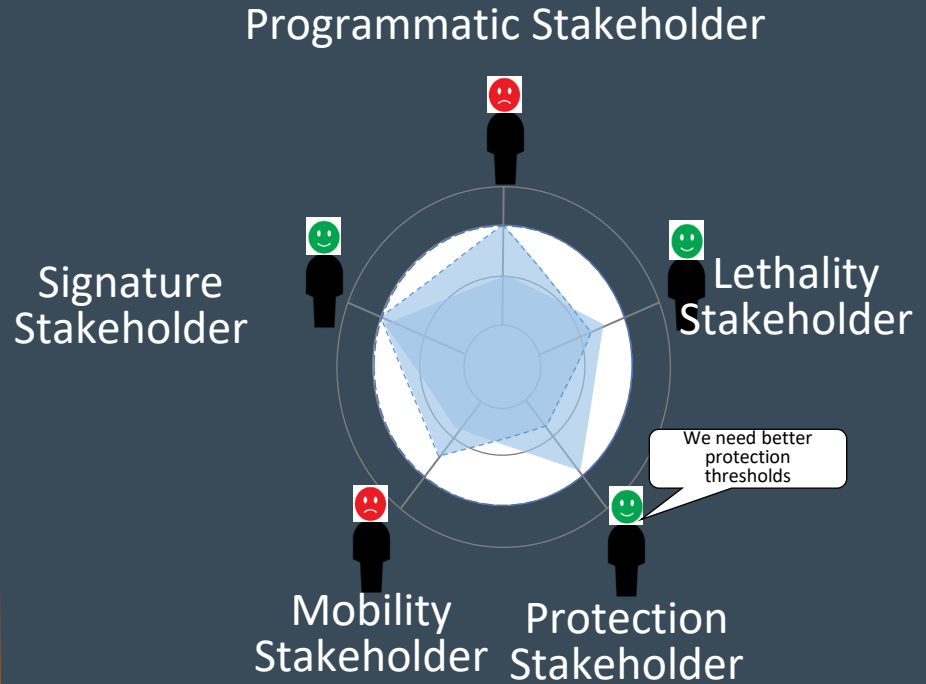
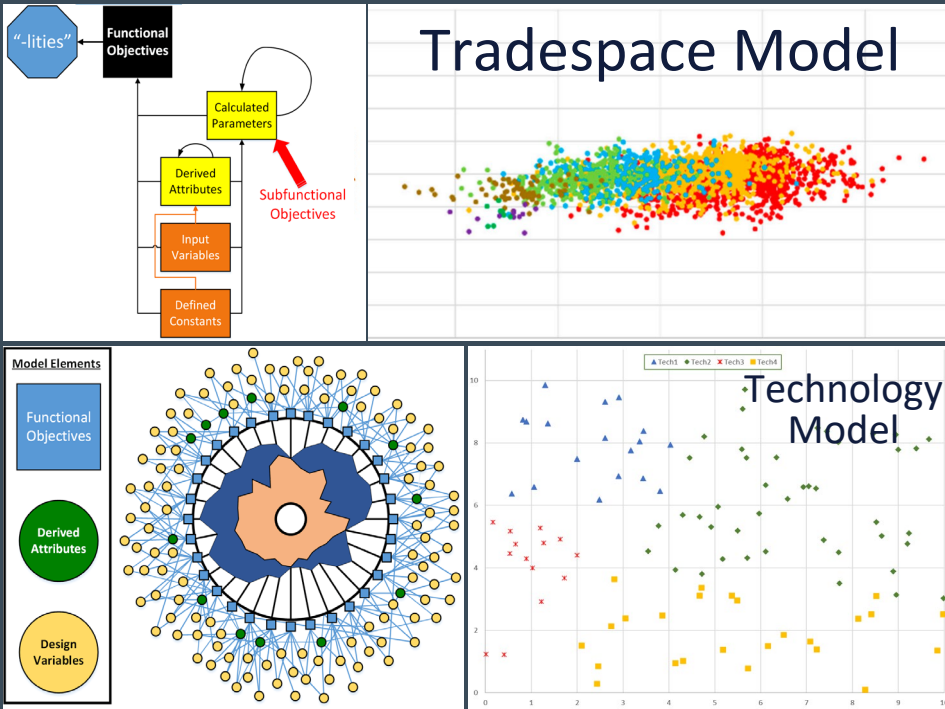
# Functional Objectives



- Functional Objectives provide metrics to evaluate the “-ilities”
  - Functional Objectives are built from
    - Calculated Parameters
    - Derived Attributes
    - Input Variables
    - Defined Constants

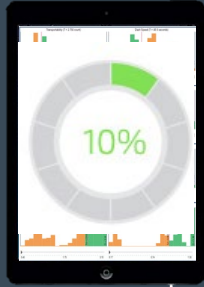


# Tradespace Decision-Making

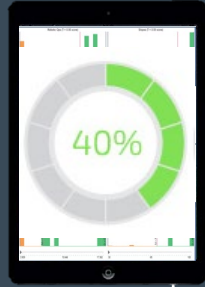


# Tradespace Decision-Making

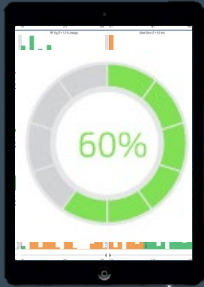
VSME 1



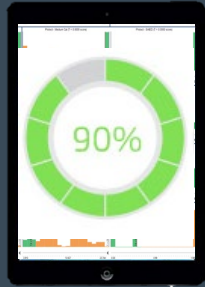
VSME 2



VSME 3

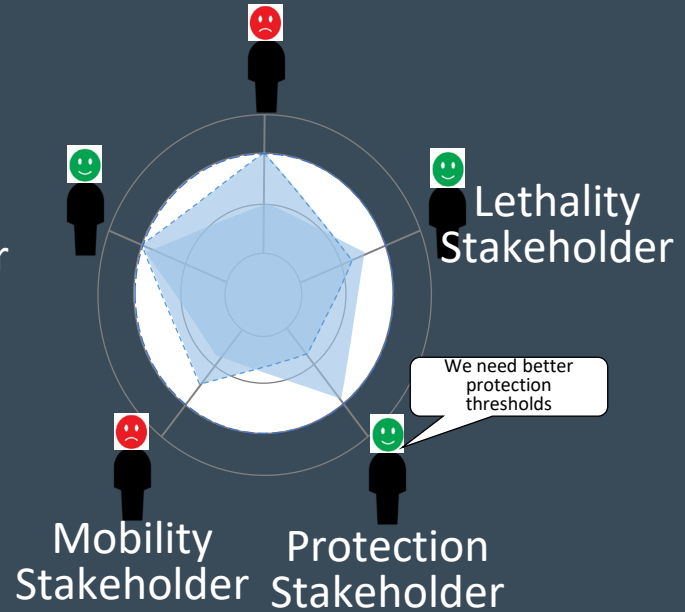


VSME 4



Programmatic Stakeholder

Signature Stakeholder



# AI Agents to the Rescue

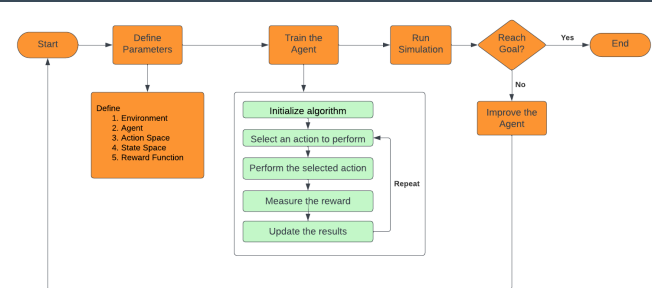
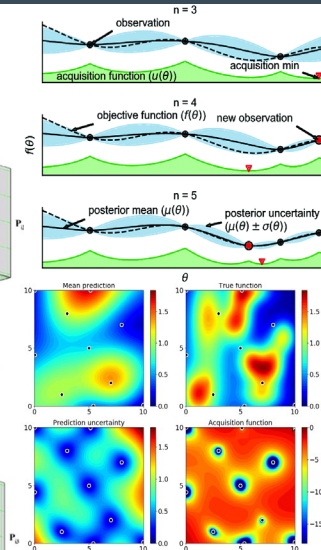
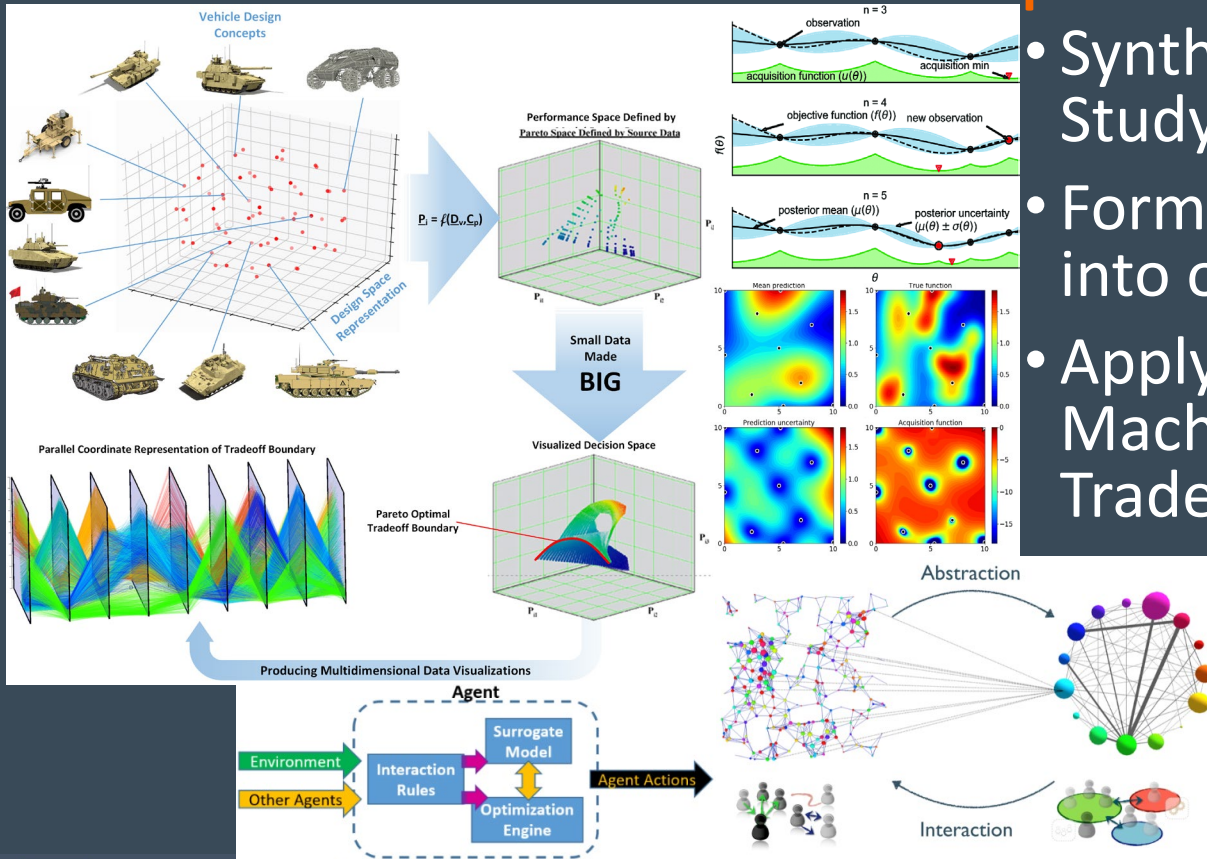
- Can we use AI Agents to simulate real decision-makers
  - With Human DMs in the Loop
  - Or, as pure simulations
- Allowing:
  - To Identify conflicts of importance in advance
  - Study the efficacy of the tradespace problem
  - Explore the downstream impacts of trades



Adapted from <https://clearcode.cc/blog/game-theory-attribution/>

# How to Accomplish This...

- Synthetic Tradespaces to Study
- Formulating tradestudies into optimization problems
- Applying Game Theory and Machine Learning Agents to Tradespace DM

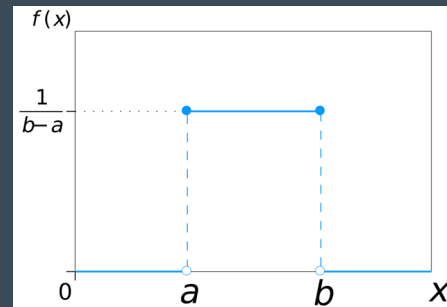


# Synthetic Tradespace: Defining Variables

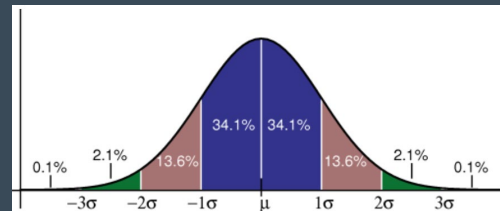
- Variables are defined using several methods
- Constant Variables
  - Have 1 known value
- Binary Variables
  - 1 if on, 0 if off
- Discrete Valued
  - Result of a selection of Binary Variables

## • Continuous Variables

- Defined by a range (uniform)



- Defined by a distribution (gaussian)



# Initial Synthetic Tradespace

- 4 Subfunctional Objectives
  - Back Deck Overhang
  - Running Gear Contact Patch Area
  - (SMET FCC) Length
  - (SMET FCC) Curb-to-Curb Turning Diameter
- Requires 54 Input Variables
  - 13 are continuous
  - 6 are discrete valued
  - 27 binary variables
  - 6 constant variables
  - 2 functional variables
- 12 Derived Attributes
- 9 Constants

# Formulating Optimization: All-in-One (AiO) MOP

$$\begin{aligned} & \text{minimize} && \mathbf{f}(\mathbf{x}_g, \mathbf{x}_{loc}) = [\mathbf{f}_1(\mathbf{x}_g), \mathbf{f}_2(\mathbf{x}_g, \mathbf{x}_{loc})] \\ \text{s.t.} &&& \mathbf{x}_g \in X_g, \mathbf{x}_{loc} \in X_{loc} \end{aligned}$$

## Goal:

1. Compute Pareto points to AiO MOP
2. Perform tradespace analysis to choose a preferred efficient design

## Strategy:

1. Decompose AiO MOP into two subproblems (SP1 & SP2)
2. Find a preferred efficient design to AiO MOP by computing efficient designs and Pareto points to SP1 & SP2

### SP1:

$$\begin{aligned} & \min \mathbf{f}_1(\mathbf{x}_g) \\ \text{s.t.} & \mathbf{x}_g \in X_g \end{aligned}$$

### SP2:

$$\begin{aligned} & \min \mathbf{f}_2(\mathbf{x}_g, \mathbf{x}_{loc}) \\ \text{s.t.} & \mathbf{x}_g \in X_g, \mathbf{x}_{loc} \in X_{loc} \end{aligned}$$

# Formulating Optimization: Coordination Problem (COP)

SP 1:

$$\begin{aligned} \min \quad & \mathbf{f}_1(\mathbf{x}_g) \\ \text{s.t.} \quad & \mathbf{x}_g \in X_g \end{aligned}$$

SP 2:

$$\begin{aligned} \min \quad & \mathbf{f}_2(\mathbf{x}_g, \mathbf{x}_{loc}) \\ \text{s.t.} \quad & \mathbf{x}_g \in X_g, \mathbf{x}_{loc} \in X_{loc} \end{aligned}$$

Let

$\mathbf{x}_g^* \in X_g$  be preferred design for SP1

$\varepsilon = (\varepsilon_1, \varepsilon_2) \geq \mathbf{0}$  be relaxation for two objectives in SP1

COP:

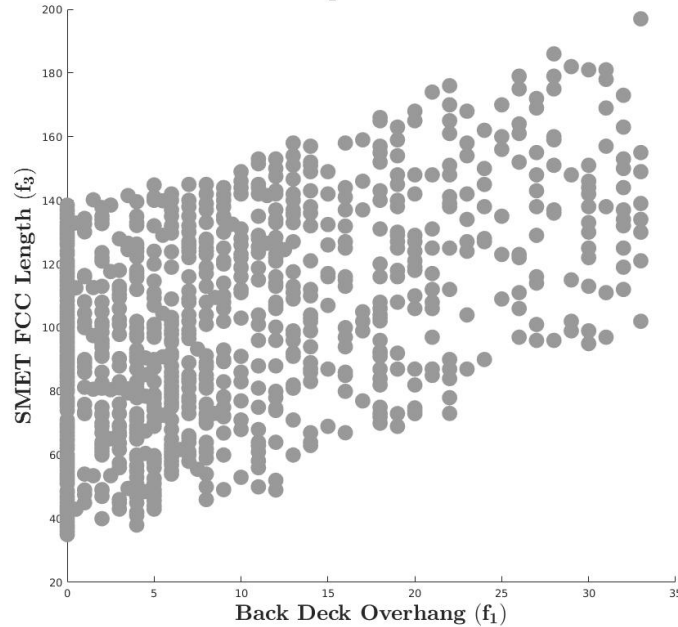
$$\begin{aligned} \min \quad & \mathbf{f}_2(\mathbf{x}_g, \mathbf{x}_{loc}) \\ \text{s.t.} \quad & \mathbf{f}_1(\mathbf{x}_g) \leq \mathbf{f}_1(\mathbf{x}_g^*) + \varepsilon \\ & \mathbf{x}_g \in X_g, \mathbf{x}_{loc} \in X_{loc} \end{aligned}$$

- Let  $\mathbf{x}_g^* \in X_g$  be weakly efficient to SP1. If there exists  $\mathbf{x}_{loc}^* \in X_{loc}$  such that  $(\mathbf{x}_g^*, \mathbf{x}_{loc}^*)$  is weakly efficient for SP2, then  $(\mathbf{x}_g^*, \mathbf{x}_{loc}^*)$  is weakly efficient for AiO MOP.
- If  $(\mathbf{x}_g, \mathbf{x}_{loc})$  is weakly efficient to COP then it is weakly efficient to AiO MOP.

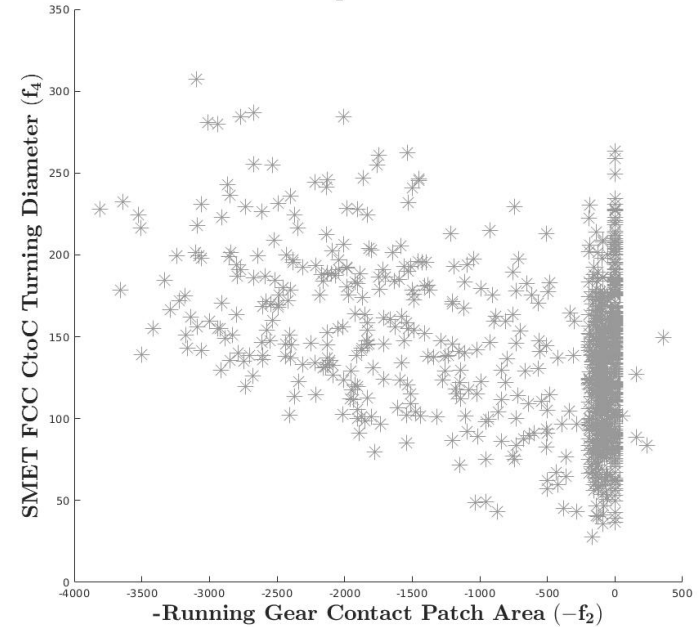


# Example: Outcome sets in Tradespaces

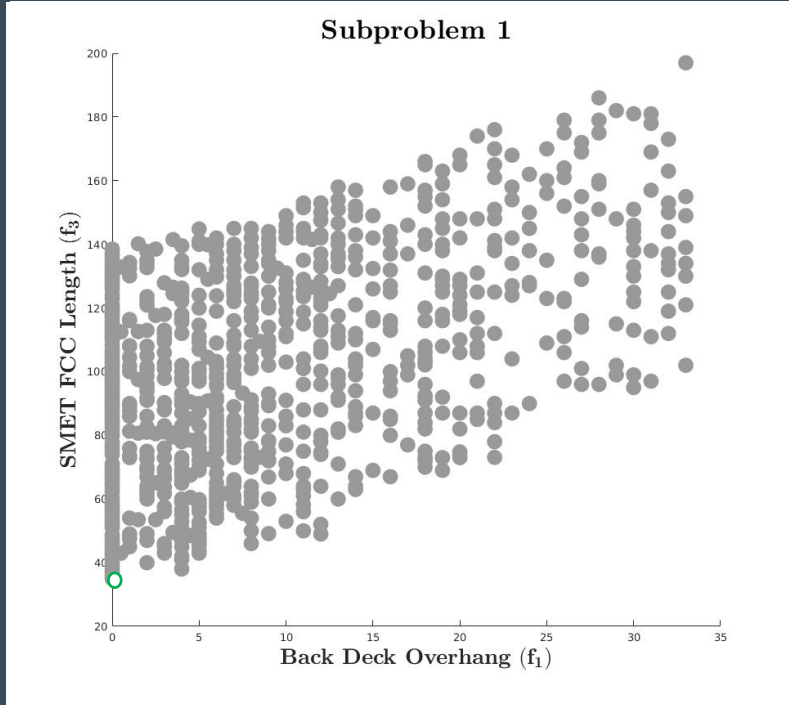
Subproblem 1



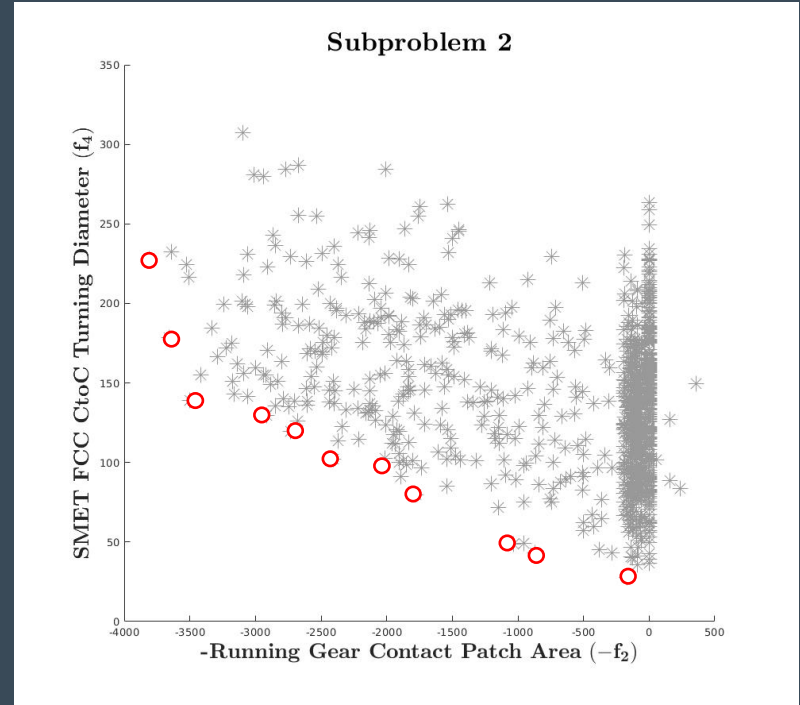
Subproblem 2



# Pareto sets in Tradespaces

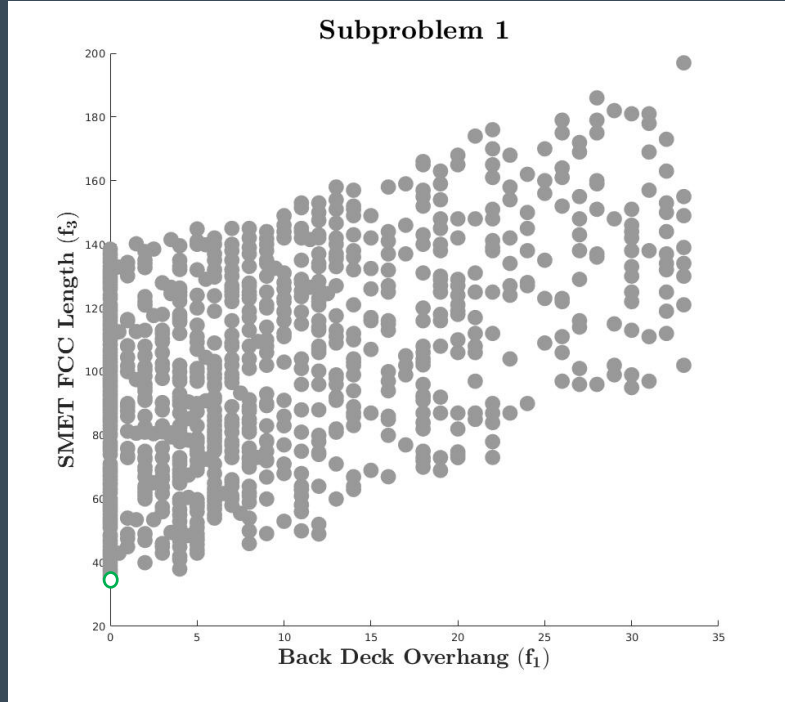


Pareto set •  
(singleton)

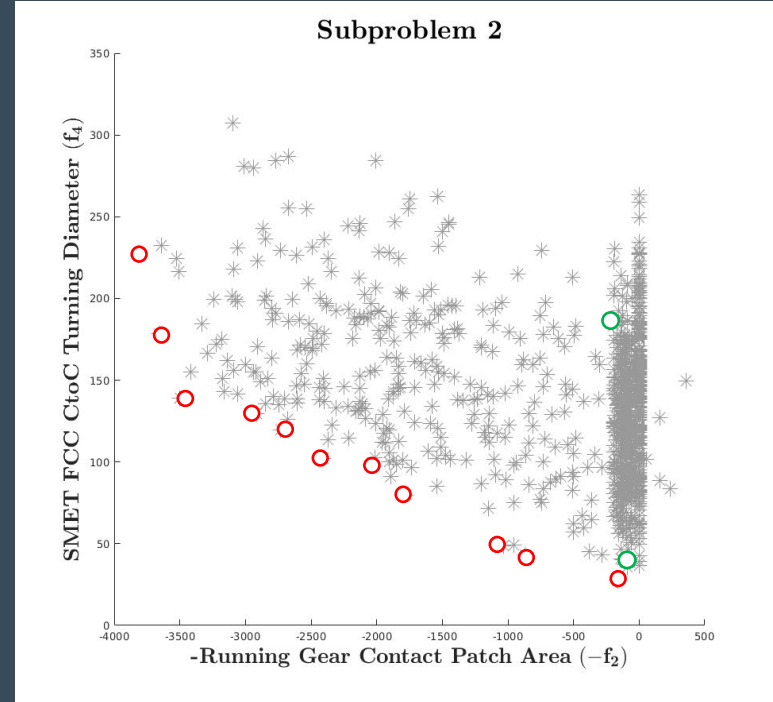


Pareto set •

# Pareto sets in Tradespaces

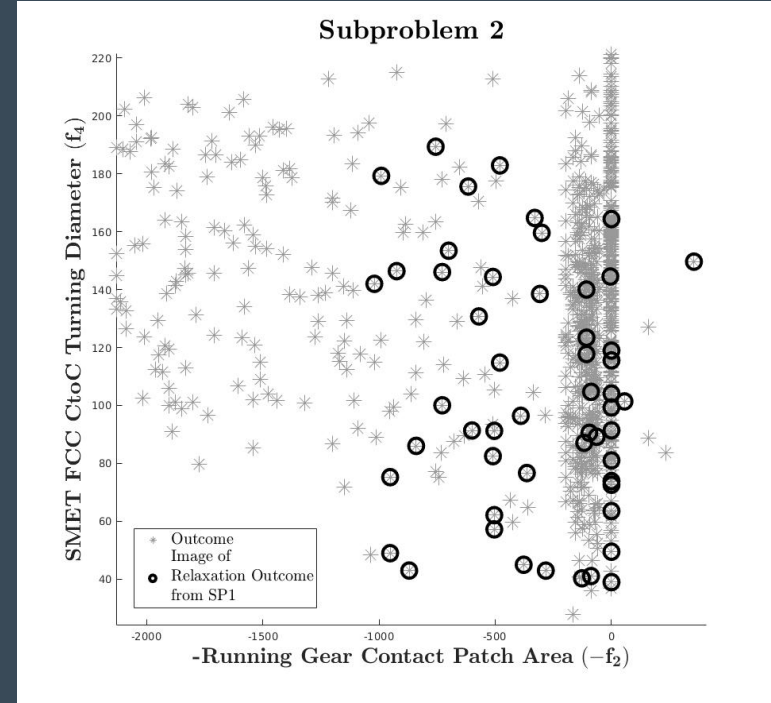
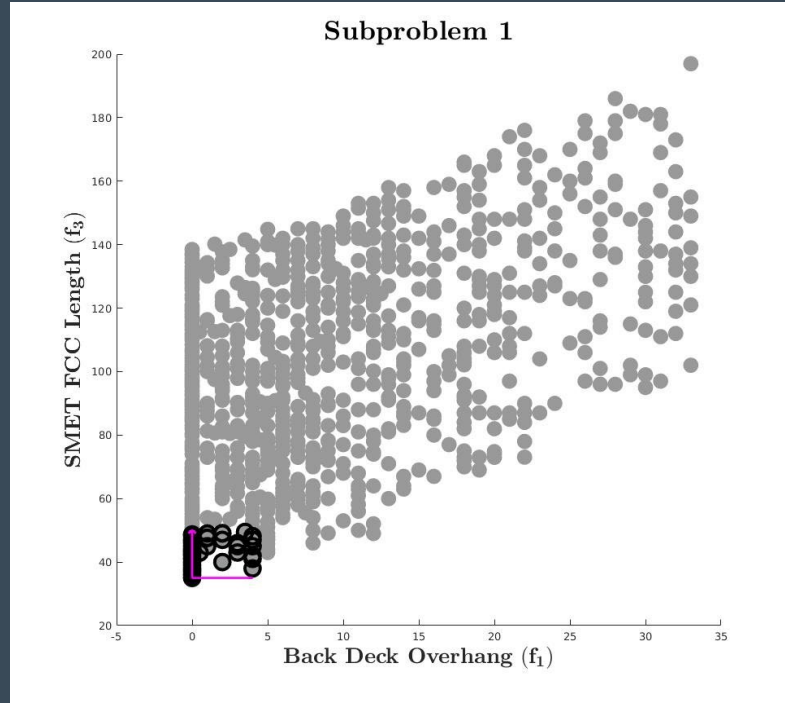


Pareto set •  
(singleton)

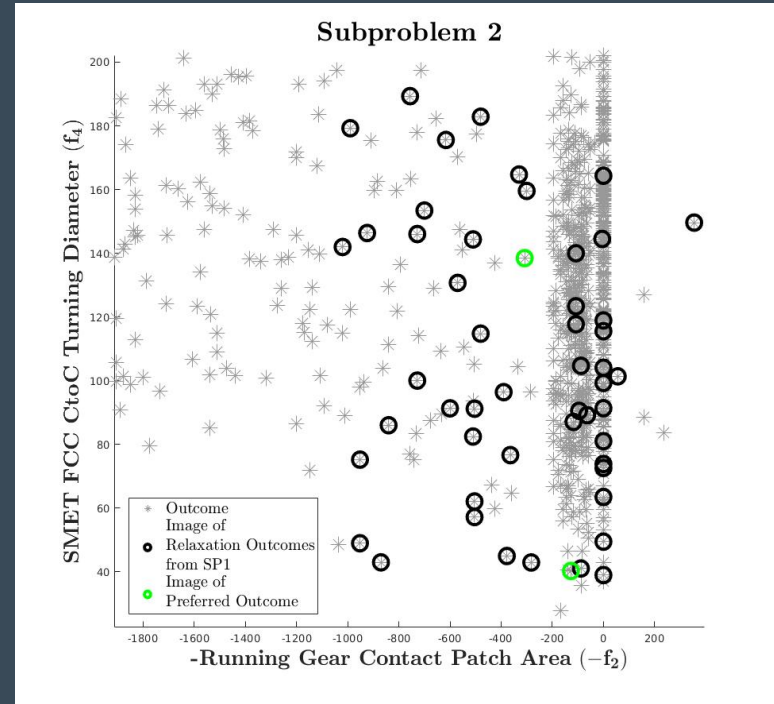
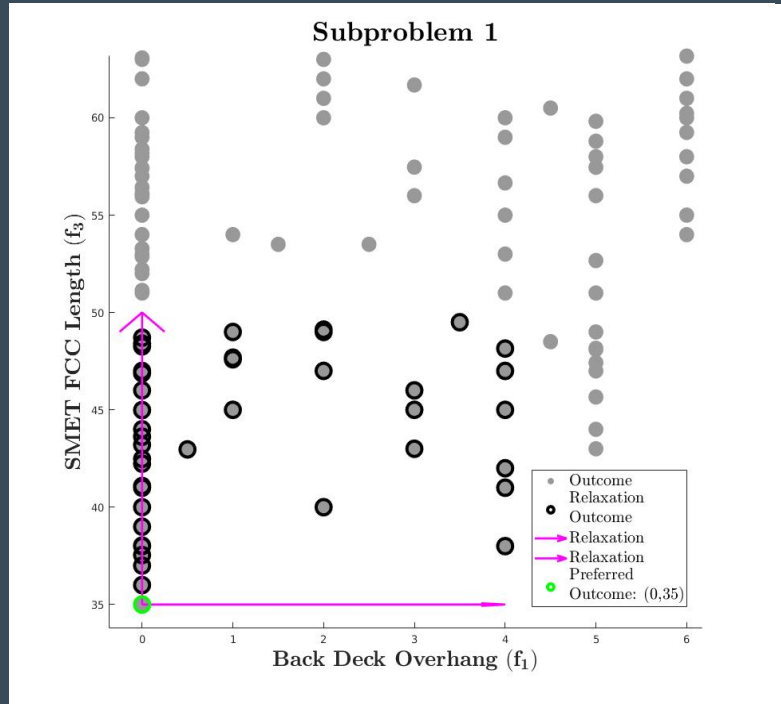


Pareto set •

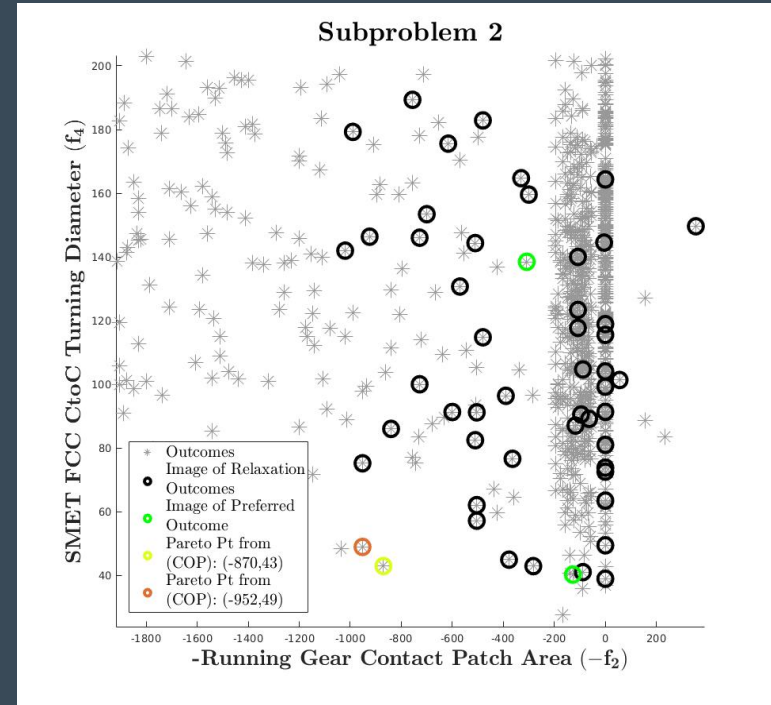
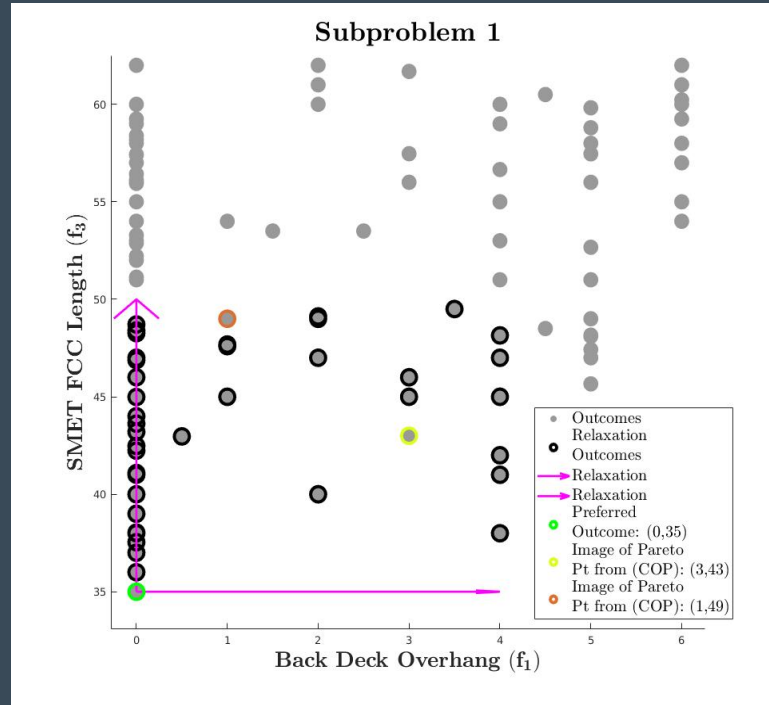
# Relaxation in Subproblem 1



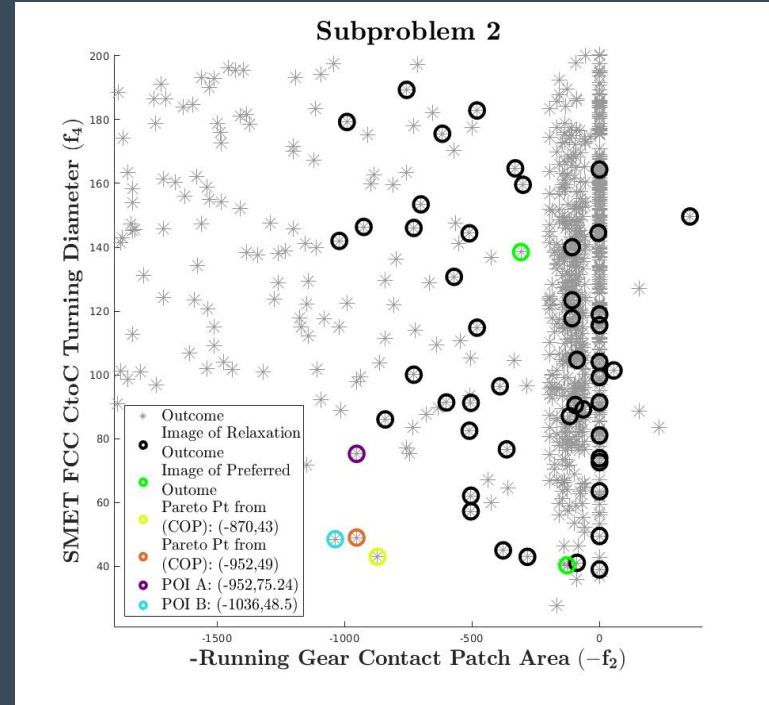
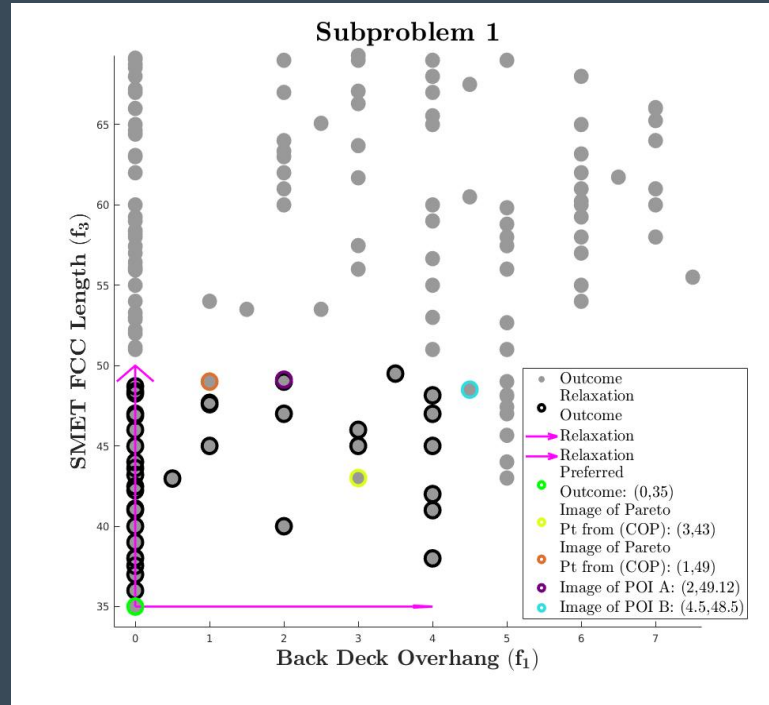
# Relaxation in Subproblem 1



# Pareto points to Coordination






# Choosing preferred Pareto point for AiO MOP



POI B = AiO preferred Pareto point

# Analysis in the design space

Preimage (design)	Pareto point for SP1 	POI A 	POI B 
Drive configuration	identical		
Total volume	similar		
Length, width, heights	different		
Includes	-	winch <b>or</b> offload generator	winch <b>and</b> offload generator



# Now comes the AI Agents

## • Current Work

- Defining and Training the Agents

***Challenge*** – Acquiring sufficient data from Decision-Makers

## • Future Work

- Once we have trained agents
  1. Can we run Human-In-the-Loop Simulations?
  2. Can we run simulated DM sessions and identify key points of contention
  3. Can we evaluate the Tradespace

# The Research Team

- **Clemson University**

- **Cameron Turner, John Wagner**

- Mechanical Engineering

- **Margaret Wiecek, Qiong Zhang, Yongjia Song**

- Mathematics

- **Philip de Castro, Hannah Stewart, Jon Charron, Aaditya Kothavade, Nate Rogers**

- Graduate Students

- **US Army Ground Vehicle Systems Center**

- **Greg Hartman**

- **Denise Rizzo**

- **David Gorsich**

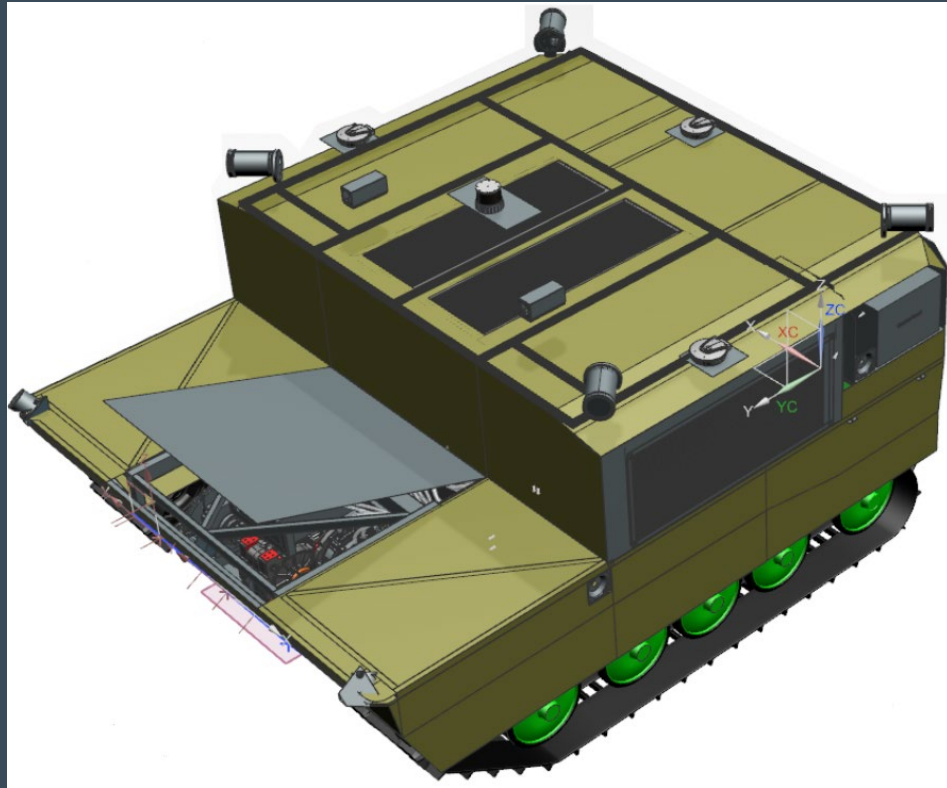
- **Annette Skowronska**

- **Rachel Agusti**

- **Matthew Castanier**

- **Stephen Rapp**

# Acknowledgements



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# Questions?

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