

# ROTORCRAFT TRADESPACE EXPLORATION INCORPORATING RELIABILITY ENGINEERING

**Sponsor: ARL**

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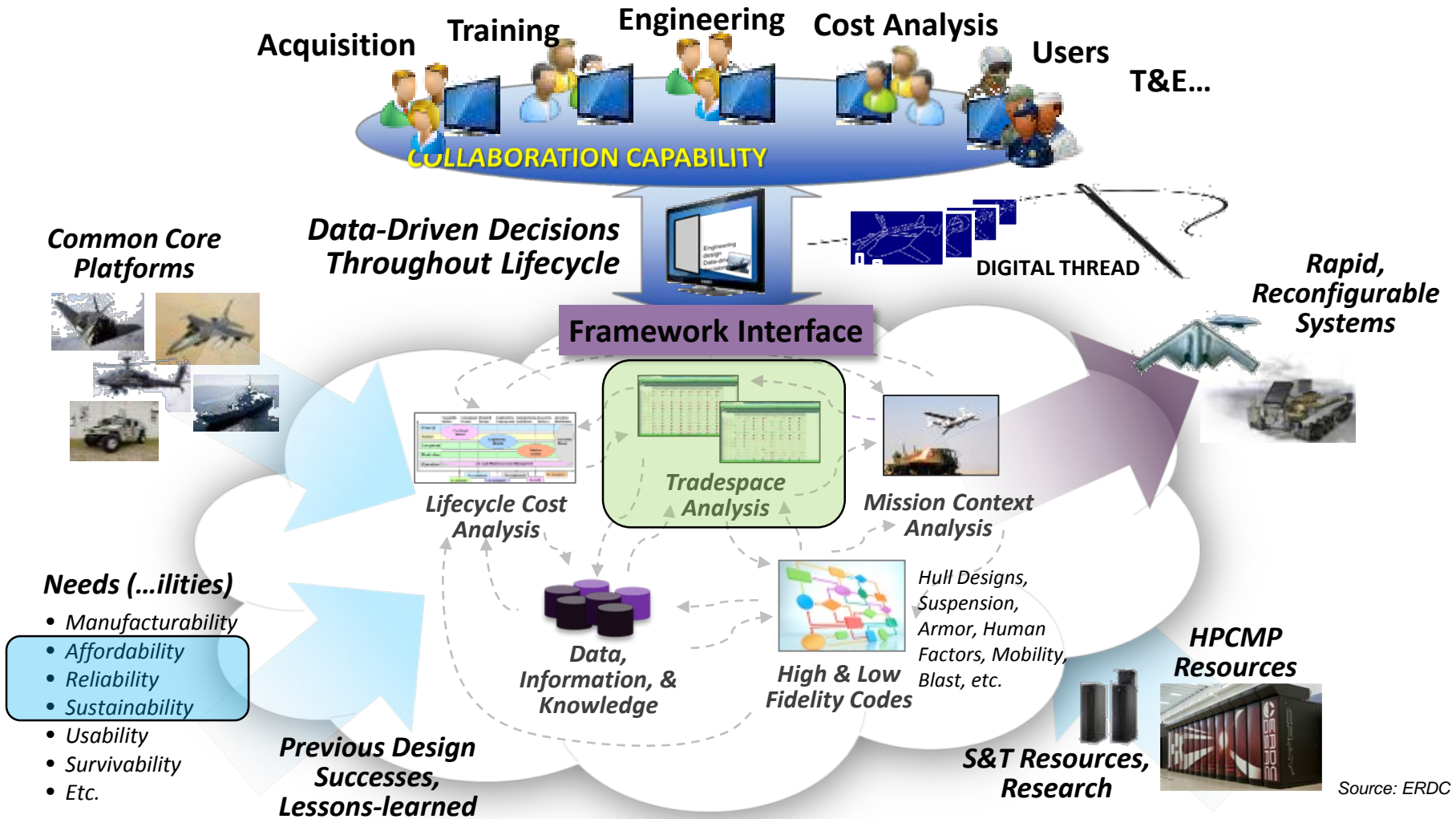
**Washington, DC 20009**

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- Background & Motivation
- Rotorcraft tradespace exploration
  - Performance covered; reliability missing
- Reliability modeling
  - Assumptions and limitations
  - Formulation
  - Results
- Summary & Conclusions
- Future work

## DOD Engineered Resilient Systems framework



Source: ERDC

- Operation and support (O&S) as well as affordability
  - Impacted by non-functional requirements (reliability, availability, and maintainability (RAM))
  - Receiving minimal tradespace consideration
- Propose strategy to incorporate reliability into tradespace exploration (TSE)
  - Develop subsystem-level reliability investment model

- Joint Multi-Role Rotorcraft Technology Demonstrator (JMR TD)
  - Intends to reduce technology transfer risk of Future Vertical Lift (FVL) initiative
- Affordability
  - Major concern in economic climate of flat and declining budgets
  - DOD needs better information and guidance to more effectively manage and reduce O&S costs

- Majority of program costs consumed during O&S
  - Essential to reduce underlying causes
  - Design for reliability (DFR)
    - Reducing part replacement costs and logistics over decades can achieve significant savings
    - Recent DOD study indicates “Many programs may underinvest in reliability early in acquisition”
  - DOD Reliability, Availability, Maintainability, and Cost Rationale Report Manual
    - Notes cost risk prominently

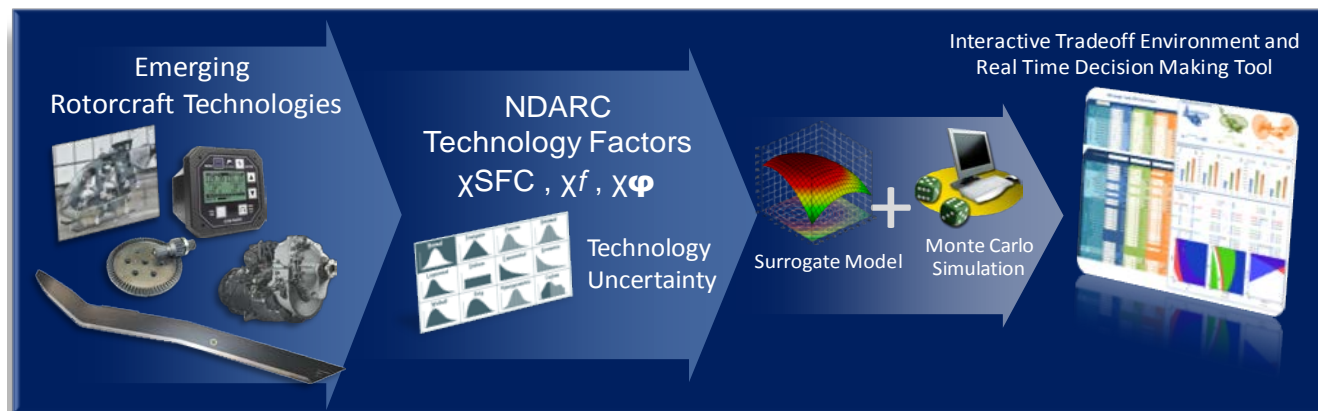
- TSE processes and accompanying tools
  - Provide intuitive environment to explore alternatives
  - Assess designs for feasibility in multiple contexts
  - Promising methodology to
    - Facilitate effective designer/stakeholder communication
    - Ensure final product with mutually agreed set of capabilities
    - Support systems engineering tradeoffs during acquisition lifecycle

- Best available TSE processes and tools research
  - Finding: ERS pilot projects omitted subject matter expert measures and stakeholder value
- Prioritizing values can
  - Enable decisions based on how well alternatives perform with respect to multidisciplinary objectives
  - Focus TSE activities
  - Achieve satisfaction within broader user-base

**RAM and affordability are highly valued by stakeholders, but are missing from TSE**



- Rotorcraft Capability Assessment and Tradeoff Environment (CATE)
  - Uses NASA Design and Analysis of Rotorcraft (NDARC)
  - Interactive assessment of technology impacts across weight, design, performance, maintenance, and cost
  - Supports introduction and assessment of new candidate technologies



Source: ARL and Georgia Tech

- Mission requirements determine vehicle size
- Configurations (single main rotor, compound, tilt rotor) assessed across 25 outputs
  - Grouped by weight, configuration, drag, propulsion, cost
  - Assess strengths and weaknesses
    - Compared to one another
    - Baseline vehicles for each category
- Lower and upper constraints on inputs reveal
  - What is possible with state of the art technologies
  - Additional logistical constraints

- Execute CATE analysis
  - Identifies designs that ensure operational effectiveness
- Vendor specific part selection
  - Performed as stakeholders form consensus
  - Makes design concepts more concrete
- High fidelity analysis
  - Considers additional design constraints
  - Quantifies performance more accurately
- Reliability analysis
  - Can be performed while part selection is in progress
- Cost and tradespace analysis
  - Incorporating reliability into TSE ensures greater attentiveness to cost**

- Crow AMSAA model
  - Strategy to achieve desired level of reliability growth over series of testing cycles
- System subject to developmental test
  - Variety of failures discovered
    - Not all of equal severity or importance
    - Simplest method divides into two categories
      - A-mode – no corrective action taken
      - **B-mode – corrective action taken**

- B-mode failures
  - $K$  – total number of failures (large unknown constant)
  - Each failure occurrence leads to system failure
    - Equivalent to series system
  - Failures discovered prior to end of testing cycle ( $T$ ) subject to fix attempt by  $T$

- System failure rate at time  $T$

$$r(T) = \lambda_A + \sum_{i=1}^K (1 - d_i) \lambda_i + (\lambda_B - \sum_{i=1}^K \lambda_i)$$

- $\lambda_A$  – Rate of A-mode failures
- $\sum_{i=1}^K (1 - d_i) \lambda_i$  – B-mode failure rate after corrective action
  - $d_i$  – Fix effectiveness of  $i^{th}$  B-mode
  - $(\lambda_B - \sum_{i=1}^K \lambda_i)$  – unobserved B-mode failures
- As  $K \rightarrow \infty$ , expected failure intensity

$$\rho(T) = \lambda_A + \lambda_B \left( (1 - \mu_d) + \frac{\mu_d}{1 + T} \right)$$

- $\mu_d$  – Average success rate of corrective actions

- Essential function failures (EFF) prevent fully mission capable (FMC) system

$$FMC = \prod_{i=1}^n (1 - EFF_i)$$

— Similar to Crow's model of B-mode failures

- MTBEFF 1/expected failure intensity

$$M(T) := \rho(T)^{-1}$$

- Cost and time required to achieve MTBEFF

$$\gamma(T) = \frac{1}{CV^2(C_0T + \mu_b \ln(1 + T))}$$

- $CV$  – Coefficient of variation in B-mode failures
- $C_0$  – Cost to operate test, analyze, and fix (TAAF)
- $\mu_b$  – Average value of cost increments incurred by corrective action



- Solving cost equation and composing with MTBEFF provides direct relationship

$$M_i(T_i) = \frac{1}{1 - \mu_{d,i} + \frac{C_{0,i}\mu_{d,i}}{\frac{1}{\lambda_{A,i}} + \frac{\mu_{b,i} F^{-1}\left(\frac{C_{0,i} + \frac{CV_i^2 \gamma_i(T_i)}{\mu_{b,i}}}{\mu_{b,i}}\right)}{\lambda_{B,i}}}}$$

- $F(W) = We^W$  - Lambert W-function

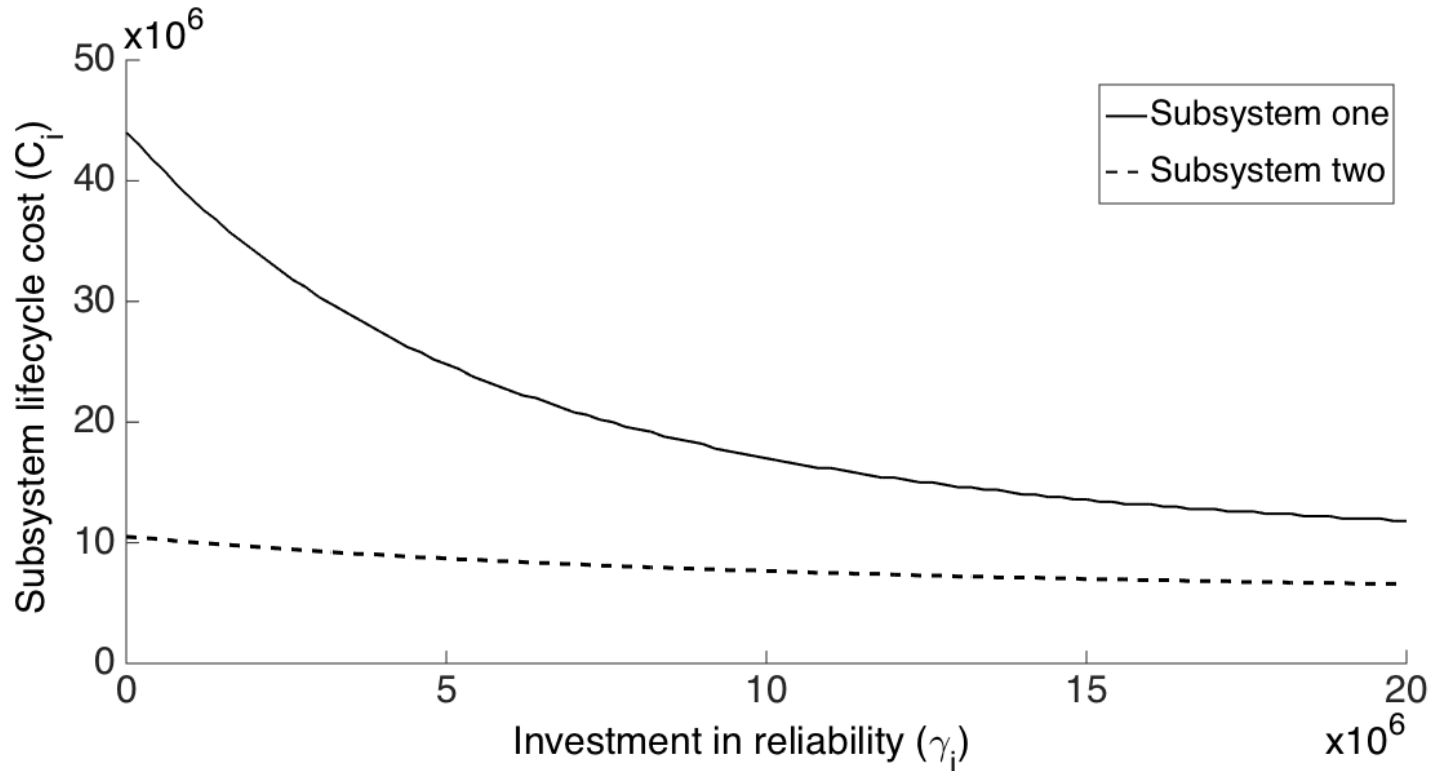
$$\max \left[ \frac{B - \sum_{i=1}^n \gamma_i(T_i)}{\sum_{i=1}^n \left( c_i \left( 1 + \left\lfloor \frac{L}{M_i(T_i)} - \varepsilon \right\rfloor \right) \right)} \right]$$

subject to  $T_i \geq 0, \forall i(1 \leq i \leq n)$

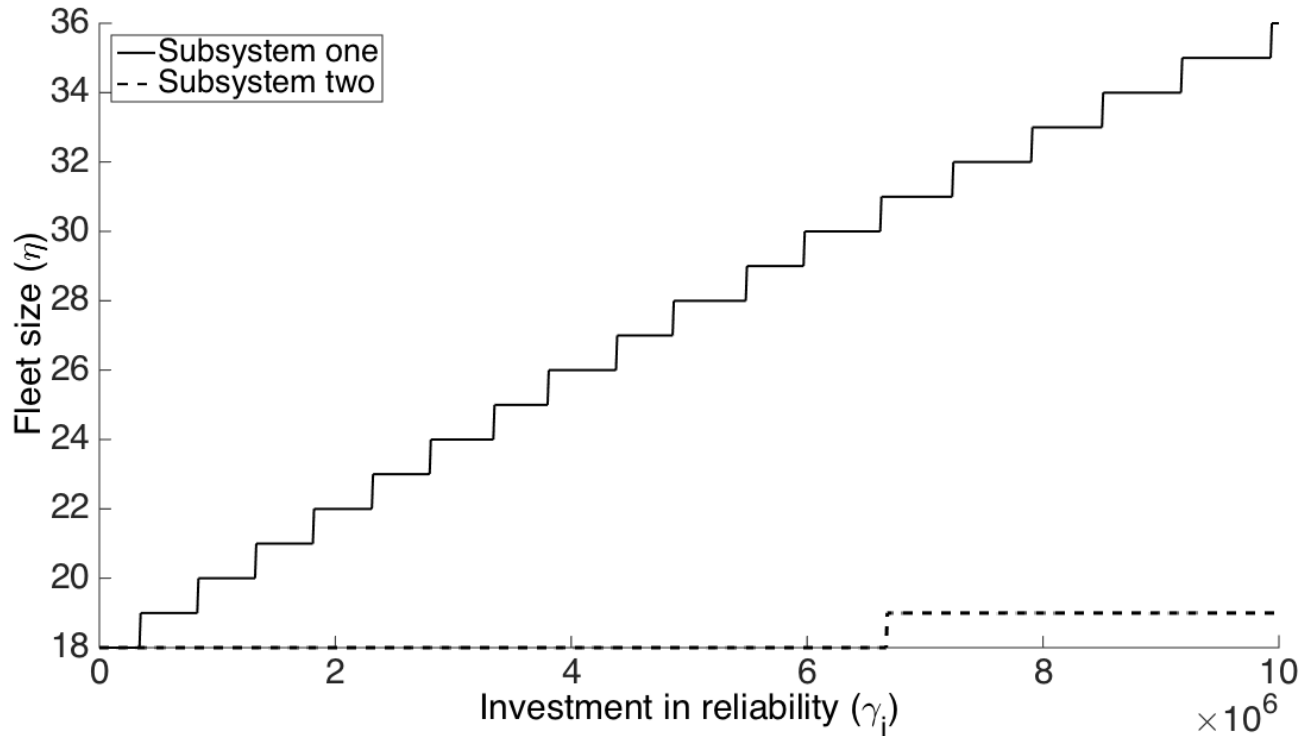
- $B$  – Total budget
- $\sum_{i=1}^n \gamma_i(T_i)$  – Subsystem reliability investments
- $c_i$  – Cost to replace subsystem  $i$  once
- $L$  – Length of system lifecycle

- Parameters chosen for sake of illustration
  - $n = 2$  subsystems
  - $B = \$1,000,000,000$
  - $L = 20,000$  flight hours

Parameters	Subsystem $i = 1$	Subsystem $i =$ 2
$M_{A,i}$ (initial A-mode failure MTBF)	1,000	500
$M_{B,i}$ (initial B-mode failure MTBF)	100	200
$C_{0,i}$ (Cost of operating TAAF)	1,000,000	800,000
$\mu_{b,i}$ (Cost of corrective action)	5,000,000	4,000,000
$\mu_{d,i}$ (B-mode fix effectiveness factor)	0.9	0.8
$c_i$ (Subsystem replacement cost)	20,000	75,000



**Subsystem one could achieve significantly greater cost savings over system lifecycle**



**Marginal investment required to improve subsystem one increases for each additional vehicle desired, but investment is preferred over subsystem two**

Parameter	No Investment	Optimal Investment
$M_1$	90.92	444.66
$M_2$	142.86	270.39
$P_1$	219	44
$P_2$	139	73
$C_1$	44,000,000	9,000,000
$C_2$	10,500,000	5,550,000
$C_s$	54,500,000	14,550,000
$\eta$	18	62
Fleet Cost	981,000,000	902,100,000

- Reliability investment results in larger fleet at lower cost
- Optimal fleet size without reliability investment:  
\$3,379,000,000  
(=62 × 54,500,000)  
—3.379x original budget

**Consideration of reliability investment could make valuable contributions to long term program affordability**

- Combine reliability engineering and TSE
  - Strategy considers investment over long term
- Studies linking reliability investment and improvement could promote
  - Compromise between performance and non-functional reliability and affordability attributes
  - Reduce lifecycle cost (LCC) and affordability

- Remove cost model assumptions
  - Office of Cost Assessment and Program Evaluation (CAPE) methodologies and tools to estimate LCC
  - LCC methodologies and tools limitations that may impede integration of tradespace methodologies and tools
- Assess fleet size and cost sensitivities to model assumptions (e.g., reliability, life, failure rate, fix effectiveness factor)



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